PERIYAR UNIVERSITY PERIYAR PALKALAI NAGAR SALEM – 636 011



DEGREE OF MASTER OF PHILOSOPHY

CHOICE BASED CREDIT SYSTEM

SYLLABUS FOR M.PHIL. STATISTICS

FOR THE STUDENTS ADMITTED FROM THE ACADEMIC YEAR 2012 – 2013 ONWARDS

Objectives:

To provide course study to postgraduates in Statistics with a view to strengthen their foundations for undertaking Ph.D work in theoretical and Applied Statistics.

Eligibility for Admission:

Good academic record with first or Second class Master Degree in Statistics of Periyar University or in examinations recognized there equivalent to.

Duration:

The duration of the M.Phil course will be one year for full time and 2 years for part time.

Course Structure:

(i) For Full time:

The M.Phil course will consist of two parts.

- Part I will be devoted to teaching of the courses. The written examination will be conducted at the end of first semester.
- **Part II** will be devoted to the writing of dissertation. Dissertation should be submitted at the end of second semester.

(ii) For Part time:

First year : course work only.

Part I : Theory examination (for all the three papers) will be held at the end of first semester in the **second year**.

Part II : Project / Dissertation evaluation at the end of II semester in the **second year.**

Course Structure for M.Phil (Statistics) Under CBCS

| | Course | Title | Exam Hours | Credit | Internal Mark | External mark | Total Marks |
|----------------------------|-----------|--------------------------------------|-------------------------|--------|-------------------|------------------|----------------|
| | Paper-I | Research Methodology | 3 | 4 | 25 | 75 | 100 |
| Part – I Semester-I | Paper-II | Advanced Statistical Inference | 3 | 4 | 25 | 75 | 100 |
| | Paper-III | Guide Paper | 3 | 4 | 25 | 75 | 100 |
| | | Total | | 12 | | | 300 |
| Part – II Semester – II | | Dissertation | Evaluation Viva-voce | 84 | By both examiners | | <u> </u> |
| | | Total | | 12 | | | 200 |
| | | Over all total | | 24 | | | 500 |

(For the candidates admitted from the year 2012-13 onwards)

Question Paper Pattern

The Question paper is divided into two parts.

PART-A consists of 5 questions, one from each unit with internal choice. Each question carries 5 marks. All questions should be answered. Total marks for PART-A is **25**.

PART-B consists of 5 questions, one from each unit with internal choice. Each question carries 10 marks. All questions should be answered. Total marks for PART-B is **50**.

Evaluation of Dissertation

| Internal Mark | | : | 50 marks |
|---|--|----------------|---|
| (For two reviews : 2 * 20 = 4 For seminar : 10 marks) | | | |
| Evaluation of Dissertation by Examiners (Internal & External) | both | : | 100 marks |
| | Total | : | 150 marks |
| Viva-Voce | | | |
| Internal Examiner | Internal Examiner | | 25 marks |
| External Examiner | | : | 25 marks |
| | Total | : | 50 marks |
| Dissertation copies to be submitted | (i) to the univ (ii) to the dep (iii) to the gu (iv) to the stu | artment ide | $ \begin{array}{cccccccccccccccccccccccccccccccccccc$ |
| | | | |

Classification of Successful Candidates:

(i) Passing Minimum:

The performance of the students is indicated by letter grades and the corresponding grade point (GP), Grade Point Average (GPA) and Cumulative Grade Point Average (CGPA)

Passing Minimum is 50% of the ESE and also 50% of the maximum of that paper.

(ii) Minimum Credits to be earned: 24 credits.

(iii) Marks and Grades:

The following table gives the marks, grade points, letter grades and classification to indicate the performance of the candidate.

| RANGE OF MARKS | GRADE POINTS | LETTER GRADE | DESCRIPTION |
|-------------------|--------------|--------------|-------------|
| 90-100 | 9.0-10.0 | 0 | Outstanding |
| 80-89 | 8.0-8.9 | D+ | Excellent |
| 75-79 | 7.5-7.9 | D | Distinction |
| 70-74 | 7.0-7.4 | A+ | Very Good |
| 60-69 | 6.0-6.9 | А | Good |
| 50-59 | 5.0-5.9 | В | Average |
| 00-49 | 0.0-4.9 | U | Re-appear |
| ABSENT | 0.0 | AAA | ABSENT |

Conversion of Marks to Grade Points and Letter Grade (Performance in a paper)

 C_i = Credits earned for course *i* in any semester.

 G_i = Grade point obtained for course *i* in any semester

n = Refers to the semester in which such courses were credited.

a) Semester:

GRADE POINT AVERAGE (GPA) = $\sum_{i} C_{i} G_{i} / \sum_{i} C_{i}$

Sum of the multiplication of grade points by the credits of the courses

GPA = -----

Sum of the credits of the courses in a semester

b) The Entire Programme:

CUMULATIVE GRADE POINT AVERAGE (CGPA) = $\sum_{n} \sum_{i} C_{ni} G_{ni} / \sum_{n} \sum_{i} C_{ni}$

| ССРА | GRADE | CLASSIFICATION OF FINAL RESULT | |
|-----------------------------|-------|-----------------------------------|--|
| 9.5 - 10.0 | 0+ | First class with Exemplary* | |
| 9 and above but below 9.5 | 0 | - Thist class with Exemptary | |
| 8.5 and above but below 9.0 | D++ | | |
| 8.0 and above but below 8.5 | D+ | First class with Distinction* | |
| 7.5 and above but below 8.0 | D | - | |
| 7.0 and above but below 7.5 | A++ | | |
| 6.5and above but below 7.0 | A+ | First Class | |
| 6.0 and above but below 6.5 | А | | |
| 5.5 and above but below 6.0 | B+ | Second class | |
| 5.0 and above but below 5.5 | В | | |
| 0.0 and above but below 5.0 | U | Re-appear | |

* The candidates who have passed in the first appearance and within the prescribed semester of the M.Phil Programme are eligible.

The maximum duration for completion of the M.Phil programme shall not exceed three years.

Commencement of this Regulation:

These regulations shall take effect from the academic year 2012-2013, ie., for students who are to be admitted to the first year of the course during the academic year 2012-2013 and thereafter.

Transitory Provision:

Candidates who were admitted to the M.Phil course of study before 2012-2013 shall not be permitted to appear for the examinations under these regulations.

SYLLABUS

M.Phil., STATISTICS

Paper I: Research Methodology

First Semester

P.Code :

(For the Candidates admitted from 2012-2013 onwards)

Unit-I

Definition of research – types of research – criteria for good research – research methods – research process.

Report writing – significance of report writing – steps involved in report writing – Types of report – layout of a report – Precautions for writing research reports.

Unit-II

Vector space over real field – subspaces – Rank of vector space and rank of matrices –Characteristic roots and vectors.

Generalized inverse – Moore & Penrose generalized inverse – existency and uniqueness. Quadratic forms – Real quadratic forms – Properties – Trace concepts & Kronecker product of matrices.

Unit-III

Probability measures –Basic concepts of probability- conditional probability. Random variables. Distribution function and their classifications.

Unit-IV

Convergence of sequence of random variables and their relationships. Radon-Nikodym theorem and its applications.

Unit-V

Characteristic function – properties. Inversion theorem and Continuity theorem. Concept of Law of Large Numbers and central limit theorem – Simple problems.

Books for Study and Reference:

| 1. Kothari. C.R. (2004) | Research Methodology, New Age International (p) Ltd. |
|---|---|
| 2. Rao. A.R. and Bhimasankaran.P. (1992) | Linear Algebra, Tata Mc Graw Hill Publishing company Ltd. |
| 3. Graybill. F.A. (1983) | Matrices with Applications in Statistics , 2 nd Edition, Wadsworth. |
| 4. Ash. R.B. (2000) | Probability and Measure theory., 2 nd edition, Academic Press. |
| 5. Bhat. B.R. (1980) 6. Billingsley. P. (1966) | Modern Probability Theory, Wiley Eastern Ltd. Probability and Measure, Wiley Publications. |

<u>QP Pattern</u>: Unit wise internal choice with maximum 75 marks Part A : 5 x 5 = 25 & Part B : 5 x 10 = 50

M.Phil., STATISTICS

Paper II : Advanced Statistical Inference

First Semester

P. Code :

(For the Candidates admitted from 2012-2013 onwards)

Unit-I

Sufficient statistics – Existence and construction of minimal sufficient statistics. Sufficiency and Completeness – Sufficiency and Invariance.

Unit-II

Minimum variance unbiased estimation. Locally minimum variance unbiased estimators. Unbiased estimation of location and scale parameters.

Unit-III

Strong consistency of Maximum Likelihood Estimators. Asymptotic efficiency of Maximum Likelihood Estimators. Best Asymptotically Normal estimators. BAN estimation for multi parameter exponential family.

Unit-IV

Uniformly Most Powerful Tests. Distributions with Monotone Likelihood Ratio. Generalization of Neymann-Pearson Fundamental lemma - LR test – Properties (asymptotic test only).

Unit-V

Unbiasedness of hypothesis testing- Similarity and completeness – UMP Unbiased tests for multi parameter exponential family.

Books for Study and Reference:

| 1. Kale. B.K. (1999) | A First Course on Parametric Inference , Narosa Publishing Co. |
|--|---|
| 2. Rohatgi. V. (1988) | An Introduction to Probability Theory and Mathematical Statistics, Wiley Eastern Ltd. |
| 3. Rao. C.R. (1985) | Linear Statistical Inference and its applications , Wiley Eastern Ltd. |
| 4. Lehmann. E.L. (1986) | Testing Statistical Hypothesis, John Wiley and Sons. |
| 5. Lehmann. E.L. (1986) | Theory of Point Estimation, John Wiley and Sons. |
| 6. Dudewicz. E.J. and Mishra. S.N. (1988) | Modern Mathematical Statistics, Wiley Eastern Ltd. |

<u>QP Pattern</u>: Unit wise internal choice with maximum 75 marks Part A : 5 x 5 = 25 & Part B : 5 x 10 = 50

MODEL QUESTION PAPER

(For the candidates admitted from 2012-2013)

M.Phil., DEGREE EXAMINATION

STATISTICS

First Semester

Paper I - RESEARCH METHODOLOGY

Time :Three hours

Maximum:75 marks

PART A - ($5 \times 5 = 25$ marks)

Answer ALL questions.

All questions carry equal marks.

1. (a) Define research. List out its types.

Or

- (b) Explain the significance of report writing.
- 2. (a) If A and B are two matrices of same order, then show that $\rho(A+B) \le \rho(A) + \rho(B)$

Or

- (b) Distinguish between linearly dependent and independent sets of vectors.
- 3. (a) Define the distribution function of random variable and state its properties.

Or

(b) Define general probability space. Mention its properties.

4. (a) show that convergence in rth mean implies convergence in probability.

Or

- (b) If $\{X_n\}$ converges in probability to X_1 and $\{X_n\}$ converges in probability to X_2 then show that X_1 and X_2 are equivalent.
- 5. (a) Define characteristic function. Write down its properties.

Or

(b) Find the characteristic function of standard Cauchy distribution.

PART B - (5 x 10 = 50 marks) Answer ALL questions. All questions carry equal marks.

6. (a) Explain in detail the criteria of a good research.

Or

- (b) Discuss the layout of a research report.
- 7. (a) Prove that the number of linear independent solutions of the equation AX = 0 is (n - r), where r is the rank of m x n matrix A.

Or

(b) Write a note on definite quadratic form X' AX. If X' AX is positive definite, then prove that

(i) det A > 0 and

(ii) every principal minor of A is positive.

8. (a) State and prove Jordan decomposition theorem.

Or

- (b) Define the empirical distribution function and its jump. Show that the number of jumps of a distribution function is almost countable.
- 9. (a) State and prove Monotone convergence theorem.

Or

- (b) Define convergence in probability and convergence in distribution. Also prove that the convergence in probability implies convergence in distribution.
- 10. (a) State and prove Inversion theorem.

Or

(b) Discuss Kolmogorov strong law of large numbers.